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PATENT

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**METHOD AND SYSTEM FOR EXTENDING
THE PERFORMANCE OF A WEB CRAWLER**

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Background of the Invention

1. Field of the Invention

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This invention generally relates to the field of search engine technology, and more particularly relates to crawlers, robots, and spiders, and to a method of improving the performance of a crawler based search engine using a proxy type device to modify hyperlink requests and HTML pages.

2. Description of Related Art

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Currently, searches on the Internet, and more specifically on the World Wide Web, are performed by users using a number of commercial search engines. These search engines are accessed at various web sites maintained by the operators of the search engines. Typically, to perform a search the user will enter terms to be searched into a form, and may also make selections from pull-down menus and checkboxes, to enter a search request on a search engine's web site. Then, the search engine will return a listing of web sites that contain the entered terms.

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Search engines perform many complex tasks which can be generally categorized as front-end and back-end tasks. For example, when the user enters the terms and executes a search, the search engine service does not immediately search the Internet or World Wide Web for web sites containing data matching the search terms. This method would be slow and cumbersome given the huge number of web site that must be searched in order to find potential matches. Instead, the search engine service will search its own internal database of cataloged terms and corresponding web sites to find matches for the entered terms. The process of accepting the user's input, searching the internal database, and displaying the results for the user would be examples of front end tasks.

However, the search engine must perform back-end tasks unseen by the user in order to create and maintain its database of terms and corresponding web sites. These back-end tasks include searching for common terms on the Internet or World Wide Web, and cataloging their locations in the search engine's internal database so that the data can be provided quickly and efficiently to users in response to a search request.

Among the devices used by search engines to find data on the Internet and the World Wide Web are robots, crawlers, and spiders. Crawlers, spiders, and robots all work in a similar manner. These devices start by issuing a hyperlink request to a web site of interest. A hyperlink request contains a Uniform Resource Locator, or URL which indicates the address to a particular web page containing data. In response to the hyperlink request, the web site will send data back to the crawler. This data may be Hyper Text Markup Language pages, known as HTML pages, or other documents. Once the crawler has

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received an HTML page, it will look for other hyperlinks contained within the HTML page itself. These new hyperlinks will be indexed and cataloged in the search engines database. Then the crawler will follow the new hyperlinks and repeat the process, collecting more hyperlinks.

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One significant limitation with current crawlers is that they only detect and follow static hyperlinks. Static hyperlinks are links in which the entire URL is plainly visible in the HTML page and easily extractable by the crawler. Some examples would include URLs such as "http://www.upsto.gov" generally following an HTML tag. HTML tags are commands written in the HTML language. Static tags would include "<A>" anchor tags, "" image tags, and "<FRAME>" child frame tags among others. Thus, the crawler will look for URLs following these tags, and extract them from the HTML document for further processing.

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However, the content on the Internet and World Wide Web that is accessible through static hyperlinks is dwarfed by the volume of content accessible via non-static hyperlinks such as those constructed from HTML forms. For example, many web pages contain a form requiring the user to enter either a selection or a keyword, and also the user may make selections via pull-down menus, checkboxes, and other selectable items. The user enters search terms and other parameter values, collectively referred to herein as parameter values, into a search engine in a web site, such as by utilizing any of the above mentioned mechanisms. In response to an input by the user, the web site will return additional data which may be in the form of an HTML page or other documents. Since existing crawlers are unable to supply this selection or keyword to the HTML form, the crawler can not reach this additional data.

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Similarly, many web sites require the use of a client side script. For instance, many web sites keep track of users who visit the site by requiring a user's identification, sometime known as a user name. Similarly, a web site may require other information such as cookies, session identifiers, catalog names, and shopping cart identifiers to name a few. Typically, this information is combined with the user's own input to the form or selection by the use of a client-side script. A client-side script is basically a set of instructions that are executed by the user's computer. Examples of such scripting languages are VBScript and JavaScript. For example, when a user visits a web site and enters data in a form, if the web site requires a user identification, a JavaScript program can intercept the request and piggyback the request with the user identification and additional information. Many web sites will not allow a user to access areas of the web site without this information. Since existing crawlers do not have the capability to handle these requests for information, they are precluded for searching the content deeper on that web site, resulting in extracting of less data and hyperlinks than possible.

Therefore a need exists to overcome the problems with existing crawlers, as discussed above, in order to access a larger amount of potentially important data on the Internet and the World Wide Web.

Brief Description of the Drawings

FIG. 1 is a system block diagram of a communication system for improving the performance of existing web crawlers in accordance with a preferred embodiment of the present invention.

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FIG. 2 is a system block diagram of a communication system for improving the performance of existing web crawlers according to an alternative preferred embodiment of the present invention.

5 FIG. 3 is a functional block diagram depicting a Proxy Engine in accordance with a preferred embodiment of the present invention.

10 FIG. 4 is a functional block diagram illustrating a more detailed view of the Search Engine Server shown in FIG. 2, according to a preferred embodiment of the present invention.

15 FIG. 5 is a functional block diagram illustrating a more detailed view of the Transcoding Engine shown in FIGs 3 and 4, in accordance with a preferred embodiment of the present invention.

20 FIGs. 6, 7, 8, and 9 comprise a flow diagram illustrating an operational sequence performed by the Proxy Engine shown in FIGs. 3 and 4, in accordance with a preferred embodiment of the present invention.

Description Of The Preferred Embodiments

25 According to a preferred embodiment of the present invention, a proxy engine, as will be discussed in detail below, overcomes problems with the prior art by providing a method and system for extending the performance of existing web crawlers. The present invention allows existing crawlers access to data on web sites that is currently unavailable to conventional crawling techniques. In contrast to requiring an entirely new crawler design, the present invention can be

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used with existing crawlers to improve their performance, requiring no changes to these existing crawlers. In accordance with the preferred embodiment, the Crawler **100** will preferably be unaware that any modification to hyperlink requests are being performed, but will be able to access data deep within web sites that currently is ignored by conventional crawler methods.

According to a preferred embodiment of the present invention, as shown in FIG. 1, a system for extending the performance of a crawler includes a Proxy Server **106** connected through a Network **102** to a Crawler **100** and a Web Site Server **104**. The Network **102** comprises a system of communication connections, such as via a local area network and/or a wide area network, and using any media such as wired, optical, wireless, or otherwise. Additionally, the Network **102** can comprise a collection of networks, such as utilized in the Internet. The Web Site Server **104** comprises a computing system implementing a server for a web site that contains HTML pages, documents, and other data of interest to the Crawler **100**.

In the exemplary embodiment shown in FIG. 1, a Proxy Engine **108** is located in a Proxy Server **106**. The Proxy Server **106** comprises a networked computing system communicatively coupled to the Network **102** and that implements the Proxy Server **106** functions and features as will be discussed in more detail below. The computing system of the Proxy Server **106** executes computer instructions required by the Proxy Server **106** functions and features and for communicating with the Network **102**. The Proxy Engine **108** will be more fully discussed in detail below.

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The Crawler **100**, in this example, is a conventional existing crawler that performs searches for hyperlinks and other data on one or more web sites accessible via at least one Web Site Server **104**. The Crawler **100** is implemented on a computing system that is communicatively coupled to the Network **102**. The computing system platform for the Crawler **100** executes computer instructions required by the Crawler **100** functions and features and for communicating with the Network **102**. In an alternative embodiment, as shown in FIG. 2, the Crawler **100** of FIG. 1 is replaced by a Search Engine Server **200**. In this example of an alternative embodiment of the present invention, a networked computing system platform for the Search Engine Server **200** encompasses the functions and features of both the Crawler **100** and the Proxy Server **106** as depicted in FIG. 1. Therefore, in the embodiment shown in FIG. 2, the Proxy Engine **108** resides on the same computing system platform as the Crawler **100**. Further, the Proxy Engine **108** is communicatively coupled to the Crawler **100**, such as via a communication interface **302** in the computing system platform.

FIG. 3 shows a more detailed view of the Proxy Engine **108**. Here the Proxy Engine **108** is shown as employing two devices, a Transcoding Engine **300** and a Method Converter **310**. The Transcoding Engine **300** maintains a bi-directional communication link via the communication interface **302** with the Crawler **100** to receive hyperlink requests from the Crawler **100** and send data including HTML pages and other documents back to the Crawler **100**. Recall that in the embodiment shown in FIG. 1, the communication interface **302** communicates over the Network **102** with the Crawler **100**. However, in the embodiment shown in FIG. 2, the communication interface **302** is

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communicatively coupled with the Crawler **100** in the computing system platform supporting both the Crawler **100** and the Proxy Engine **108**.

5 Additionally, the Transcoding Engine **300** maintains a second bi-directional communication link via a second communication interface **304** over the Network **102** with the Web Site Server **104**. The second communication interface **304** is used to send hyperlink requests to the Web Site Server **104** and receive data including HTML pages and other documents from the Web Site Server **104**. The Transcoding Engine **300** also maintains a bi-directional
10 communication interface **306** internal to the Proxy Engine **108** to send hyperlink requests from the Transcoding Engine **300** to the Method Converter **310** and to receive data including HTML pages and other documents from the Method Converter **310**. Finally, the Method Converter **310**, also includes a bi-directional communication interface **312** to communicate via the Network **102** with at least
15 one Web Site Server **104**. This communication interface **312** is used by the Method Converter **310** to send hyperlink requests to a Web Site Server **104** and receive data including HTML pages and other documents from the Web Site Server **104**. The Method Converter **310**, according to a preferred embodiment of the present invention, converts a GET method hyperlink request to a POST
20 method hyperlink request, and handles POST method hyperlink request communications with the Web Site Server **104**. For example, the resulting data sent from the Method Converter **310** to the Web Site Server **104** would be a single HTTP request. Contained within that request would be a single static hyperlink. Also contained in that request, separate from the hyperlink, would be
25 additional data that would normally be included in a GET method hyperlink. The Web Site Server **104** that requires a POST method hyperlink request will receive such data in the POST method hyperlink request and then respond to the

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Method Converter **310** with data, such as HTML pages and other documents. A method conversion proxy function, via the Method Converter **310**, typically receives a GET method hyperlink request, then the Method Converter **310** extracts the "url" parameter of the request, and further extracts the CGI parameters encoded in the request, and connects to the Web Site Server **104** that is indicated by the "url" parameter. Then, after connecting, the Method Converter **310** passes the CGI parameters to the Web Site Server **104** using the POST method, and receives the Web Site Server **104** response. The response is then passed on to the Transcoding Engine **300**. The Transcoding Engine **300** processes the response data and then sends the data, such as in an HTML page document and/or other documents, back to the Crawler **100**.

As shown in FIG. 4, an alternative preferred embodiment of the present invention contemplates the Proxy Engine **108** residing on the same computing system platform or at the same location as the Crawler **100**. In contrast to the embodiment shown in FIG. 1 where the Proxy Engine **108** communicates with the Crawler **100** across the Network **102**, in this alternative embodiment the Search Engine Server **200** includes the Crawler **100** and the Proxy Engine **108**, such as on the same networked computing system. Therefore, the communication interface **302** used by the Transcoding Engine **300** to communicate with the Crawler **100** is internal to the Search Engine Server **200** without accessing the Network **102**. According to a preferred embodiment of the present invention, this interface **302** comprises an inter-application communication interface, such as supported in modern operating systems, to allow a first application, such as the Proxy Engine **108**, to communicate with a second application, such as the Crawler **100**, both applications being hosted on the same computing system platform of the Search Engine Server **200**. The

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communication interface **302** normally receives hyperlink requests from the Crawler **100** and sends data, including HTML pages and other documents, back to the Crawler **100**.

5 As depicted in FIG. 5, the Transcoding Engine **300** includes a Transcoder, **500**, and either a Script Engine **502**, a Script Filter **506**, or both. The Script Engine **502** maintains a bi-directional communication interface **504** with the Transcoder **500** internal to the Transcoding Engine **300** to receive requests to execute scripts, and return parameter values to the Transcoding Engine **300**.
10 According to a preferred embodiment of the present invention, the Script Engine **502** takes a list of synthetic hyperlinks produced by the Transcoder **500** plus a script code that is defined in an HTML page. For each hyperlink, the Script Engine **502** executes functions of the script code and produces an output. This output may be identical to or different from the original synthetic hyperlink,
15 depending on the actions of the script code. The modified set of hyperlinks is returned to the Transcoder **500**.

 In similar fashion to the communication with the Script Engine **502**, the Script Filter **506** maintains a bi-directional communication link **508** with the
20 Transcoder **500** internal to the Transcoding Engine **300**. This bi-directional communication link **508** is used to send requests to the Script Filter **506** to generate parameter values to be sent back to the Transcoder **500**. The Script Filter **506** handles script code of at least one particular Web Site Server **104**.
25 The Script Filter **506** analyzes the script code of an HTML page and performs the actions described in the script code without actually executing them in a script engine. This analysis is preferable over actual execution of script code in

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certain situations. For example, it may be preferable to analyze script code when

a) execution would be slow, such as due to a very large amount of script code, or
b) the script engine is not able to execute the script code due to incompatibility
5 with the script language version, or c) if the script engine is not available. The
Script Filter **506** accepts as input a set of synthetic hyperlinks generated by the
Transcoder **500**, plus the script code defined in an HTML page. For each
hyperlink, the Script Filter **506** performs a computation defined by one or more
filters to output a modified set of hyperlinks. The modified set of hyperlinks is
10 then returned to the Transcoder **500**.

The general operation of the Proxy Engine **108** according to a preferred
embodiment of the present invention is illustrated in FIGs. 6 through 9. FIG. 6,
and continuing on FIG. 8 and FIG 9, comprises functions of the Transcoding
15 Engine **300**. FIG. 8 illustrates exemplary functions of the Script Engine **502**.
FIG. 9 shows functions of the Script Filter **506**. FIG. 7 comprises exemplary
functions of the Method Converter **310**.

Referring to FIG. 6, the Transcoding Engine **300** receives a hyperlink
20 request from the Crawler **100**, at step **600**. The hyperlink request may comprise
a static hyperlink and/or a synthetic hyperlink. Synthetic hyperlinks are
hyperlinks that have been created by the Transcoder **500** and inserted into an
HTML page that are sent back to the Crawler **100**. Upon receiving the hyperlink
request, the Transcoder **500** determines whether the hyperlink is a synthetic
25 hyperlink requiring method conversion, at step **602**. If the hyperlink requires
method conversion, the Transcoder **500** will have specially marked the synthetic
hyperlink before inserting the synthetic hyperlink into an HTML page and sending

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it back to the Crawler **100**. Synthetic hyperlinks marked for method conversion will be sent to the method converter, at step **606**, via the communication interface **306**.

5 If the hyperlink or synthetic hyperlink does not require method conversion, it is sent to a Web Site Server **104** across the Network **102**. In response to locating the web site indicated by the hyperlink or synthetic hyperlink request, the Web Site Server **104** will send the first page or document, at step **604**, to the Transcoder **500** via the communication interface **304**. The Transcoder **500** will
10 then analyze the data returned from the web site. If the data is a document other than an HTML page, the document will be sent directly to the Crawler **100** via the communication interface **302**. If the data is an HTML page, the Transcoder will determine whether the web site uses any form inputs from analyzing the HTML page, at step **608**. If there are no form inputs indicated in the HTML page, the
15 data received from the web site is sent back, at steps **610**, **611**, to the Crawler **100** and exiting the transaction until a further hyperlink request is sent to the Transcoder **500**.

Recall that many web pages contain a form requiring a user to enter either
20 a selection or a keyword, and also a user may make selections via pull-down menus, checkboxes, and other selectable items. The user can enter search terms and other parameter values, collectively referred to herein as parameter values, into a search engine in a web site, such as by utilizing
any of the above mentioned mechanisms. In response to an input by the
25 user, the web site will return additional data which may be in the form of an HTML page or other documents.

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If the Transcoder **500** determines that the HTML page contains a form, it will generate parameter values for the form, at step **612**. A form input can be implemented in a number of ways. For instance, some web sites allow a user to make a selection of a number of choices. These would be indicated on the HTML page by the use of the HTML tag "<INPUT>", "<OPTION>" or "<SELECT>" followed by various choices. The Transcoder **500** can examine the HTML page for these tags and the various choices following the tags. In this way, the Transcoder **500** can determine appropriate parameter values to be used in the form on the HTML page.

Similarly, a form may be implemented as a box for text entry by the user. One method of indicating the use of a text entry on the HTML page is by the use of the HTML tag "<INPUT TYPE=TEXT>". If the Transcoder **500** detects use of this HTML tag, it will look for a default text value in the HTML page and it will use this text value as an appropriate parameter value. If the Transcoder **500** can not find a default value, it will generate parameter values, at step **612**, to be used for creating the synthetic hyperlinks using the individual letters A through Z, the individual numbers 0 through 9, and other values selected from a list of common nouns.

After generating parameter values for any forms, the Transcoder **500** will augment the hyperlink request with the parameter values, creating one or more synthetic hyperlink, at step **614**. Furthermore, script analysis is performed in conjunction with the HTML form analysis. The Transcoder **500** first determines if the HTML page contains a script, at step **616**, such as a Java Script. If no scripts are present in the HTML page, the Transcoder must determine if the

synthetic hyperlink requires method conversion, at step **806**, as shown in FIG. 8 and in FIG. 9.

When a form is used on a web site, a user's input is transmitted to the web site using several different methods. Two typical methods are the GET and POST methods. When a GET method is used, the hyperlink is constructed by the user's browser wherein the hyperlink is a combination of the base URL and the user's input. In contrast, when using a POST method, the base URL and the user's input will be transmitted separately. Since most existing crawlers can only handle the GET method, synthetic hyperlinks destined for web sites using the POST must be converted to the POST method. To indicate to the Transcoder **500** which synthetic hyperlinks require conversion, the Transcoder **500** must decide which synthetic hyperlinks require conversion, at step **806**, and specially mark those hyperlinks, at step **808**. After the synthetic hyperlinks that require conversion are marked, the synthetic hyperlinks are combined with the data from the web site, at step **810**. Generally, the synthetic hyperlinks are inserted into the HTML page from the web site. Finally, the combined data is sent back to the crawler, at step **812**, for further processing.

If, however, the Transcoder **500** determines that there are scripts present in the HTML page, at step **616**, the Transcoder will use one of several devices to generate parameter values required by the script. Two such devices are shown in FIG. 5: The devices are the Script Engine **502** and the Script Filter **506**. An exemplary function of the Script Engine **502** according to the preferred embodiment of the present invention is shown in FIG. 8, where the Transcoder **500** invokes the use of a Script Engine **502**. The Script Engine **502** will execute the script indicated in the HTML page, thereby generating parameter values

required by the web site, at step **802**. On the other hand, an alternative method of using a Script Filter **506** is shown in FIG. 9. In contrast to the Script Engine **502** one implementation of the Script Filter **506**, in accordance with the preferred embodiment of the present invention, selects parameter values by consulting a
5 list or table of appropriate values determined by examining the various script instructions on the HTML page, at step **900**. These parameter values are selected without actually executing the script present in the HTML page.

After the parameter values have been determined by either the Script
10 Engine **502** or the Script Filter **506**, the synthetic hyperlink is augmented with the parameter values, at steps **804, 902**. Accordingly, the Transcoder **500** decides which synthetic hyperlinks require conversion, at step **806**, and specially marks those hyperlinks, at step **808**. After the synthetic hyperlinks that require conversion are marked, the synthetic hyperlinks are combined with the data from
15 the web site **810**. Generally, the synthetic hyperlinks are inserted into the HTML page from the web site. Finally, the combined data is sent back to the crawler, at step **812**, for further processing.

In a preferred embodiment of the present invention, when a hyperlink
20 request is made by the Crawler **100**, the Transcoder **500** determines whether the hyperlink request is a synthetic hyperlink and if it is marked for method conversion, at step **602**. If a synthetic hyperlink requires method conversion, the Transcoder **500** sends the synthetic hyperlink to the Method Converter **310**. Recall that the Transcoder **500** has already determined what method is used by
25 the destination web site and has marked the synthetic hyperlink accordingly, at step **808**. The Method Converter **310** converts the synthetic hyperlink to the method indicated in the synthetic hyperlink itself, at step **700**. The synthetic

hyperlink is then sent to the Web Site Server **104** using the method required by that web site, at step **702**. In response to the synthetic hyperlink request, a Web Site Server **104** will return the requested data which is received, at step **704**, at the Method Converter **310**. Thereafter, the Method Converter **310** will send the data from the web site back to the Transcoder **500** for further processing. In a preferred embodiment of the present invention, further processing will begin with a determination of whether data from the web site contains a form, at step **608**, as has been described above.

The Proxy Engine **108** can be realized in hardware, software, or a combination of hardware and software. A Transcoding Engine **300** and a Method Converter **310**, as illustrated in FIG. 3 according to a preferred embodiment of the present invention, can be realized in a centralized fashion in one computer system, or in a distributed fashion where different elements are spread across several interconnected computer systems. Similarly, the invention consisting of an aforementioned Transcoding Engine **300** and a Method Converter **310** can be combined with the Crawler **100** on the same computing system platform, server, computer or other implementation as illustrated in FIG. 2, or they may be distributed across several interconnected computing systems, one such configuration being illustrated in FIG. 1.

Furthermore, any kind of computer system platform, or other apparatus adapted for carrying out the methods described herein, is suited for implementing the Proxy Engine **108**, as will be anticipated by those of ordinary skill in the art in view of the discussion above. A typical combination of hardware and software could be a general-purpose computer system with a computer

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program that, when being loaded and executed, controls the computer system such that it carries out the new and novel methods described herein.

5 The Proxy Engine **108** can also be embedded in a computer program product, which comprises features and functions enabling the implementation of the new and novel methods described herein, and which - when loaded in a computer system - is able to carry out these methods. Computer program means or computer program in the present context mean any expression, in any language, code or notation, of a set of instructions intended to cause a system
10 having an information processing capability to perform a particular function either directly or after either or both of the following a) conversion to another language, code or, notation; and b) reproduction in a different material form.

Each computer system may include, inter alia, one or more computers
15 and at least a computer readable medium allowing a computer to read data, instructions, messages or message packets, and other computer readable information from the computer readable medium. The computer readable medium may include non-volatile memory, such as ROM, Flash memory, Disk drive memory, CD-ROM, and other permanent storage. Additionally, a computer
20 medium may include, for example, volatile storage such as RAM, buffers, cache memory, and network circuits. Furthermore, the computer readable medium may comprise computer readable information in a transitory state medium such as a network link and/or a network interface, including a wired network or a wireless network, that allow a computer to read such computer readable
25 information.

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Although specific embodiments of the invention have been disclosed, those having ordinary skill in the art will understand that changes can be made to the specific embodiments without departing from the spirit and scope of the invention. The scope of the invention is not to be restricted, therefore, to the
5 specific embodiments, and it is intended that the appended claims cover any and all such applications, modifications, and embodiments within the scope of the present invention.

What is claimed is:

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